

Research Article

# A Comparative Study of Rectangular Beam Depth Effects Under EBCS-1995 and ES EN-2015 Codes

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## Abstract

To achieve structural integrity, serviceability, and economy of buildings, national and international building standards are used for dimensioning and proportioning of structural members. Building codes may be amended due to, the existence of new construction materials, technologies, and structures, and to improve earlier gaps. Ethiopia has experienced three building codes in the last 40 years. Those codes were the Ethiopian Standard Code of Practice, ESCP 1983-1995, Ethiopian Building Code of Standard, EBCS-1995, and the Ethiopian Standard, ES EN 2015. Design code compliance design and supervision of buildings is one of the major ways to achieve the planning, design, construction, service life as well as overall performance of projects. This study is conducted on the depth determination of an interior RC beam with different span and steel grades under EBCS-1995 and ES EN-2015 design codes. The result of this study proves that EBCS 1995 is uneconomical for shear and moment design for longer spans, and preferable for smaller spans, while ES EN 2015 provides smaller serviceable depth and deflection and maintains economical design for longer spans. Construction professionals need to understand the basic purpose of code amendment and should use the new design code as a major design reference and the earlier code accordingly.

## Keywords

Effective Depth, Serviceability Depth, Ultimate Depth, Span-to-Depth Ratio, Design Code

## 1. Introduction

The structural strength, serviceability, as well as economy of a reinforced concrete structure, primarily depend on the geometric dimension of a member aligned with the quality of the material, the function of the structure, and the load expected to be resisted. According to [1] the influence of prestressing TRM on bearing capacity, fracture characteristics, and ductility 3 RC beam was studied experimentally and it was concluded that the crack load, yield load, and ultimate load can be significantly increased by prestressing TRM reinforcement, and the yield load can be increased by more than 30%. Based on the study [2] conducted numerical and ex-

perimentally investigation on the performance of reinforced concrete (RC) beams with unequal depths subjected to combined bending and shear and the results confirmed that geometric properties(shape and depth) affect the cracking, yielding level, ultimate load carrying capacity and mode of failure modes. The side effects on beams with small shear span-to-depth ratios less than 1.15 using finite element modeling technics are investigated and the results indicate for shear span-to-depth ratio less than 1.15, the size of the beam doesn't have effect [3]. The effect of beam depth on the performance of shear-deficient beams externally strengthened

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with carbon fiber-reinforced polymer composites was investigated on parameters like ductility, cracks, and failures, and the results showed that externally bonded carbon fiber-reinforced polymer increased the shear capacity of the beam [4]. The effect of various concrete grades on composite members of framed structures experimentally using rolled steel sections as reinforcement cast was studied. According to his findings the results of failure loads and deformations in flexure and axial compression show that, the use of rolled steel sections as reinforcement proves to be advantageous even for variations in grades of concrete [5]. The effect of Cross Section Dimensions on Stiffness and Deflection on Reinforced Concrete Beams using the Response-2000 application program was studied to determine deflection values, maximum load, crack width, and stiffness by modeling 10 beam specimens with dimensional variations but the same cross-sectional area. The results of the study show that beams with the same surface area but different shapes of different dimensions greatly affect the deflection value, maximum load, crack width, and stiffness [6]. The research study [7] indicates that the minimum thickness based on ACI recommendation for a fixed-ended beam under a given grade of steel and concrete is  $L/21$ . The authors studied the Comparison of design calculations of Deep beam design using three codes namely the Indian standard code, the American Concrete Institute code, and the Construction Industry Research and Information Association code. The author noted that, for structural members exposed to public view or environmental elements, the serviceability performance of the structure is arguably as significant as its strength. After a detailed comparison, he concludes that the Indian standard code gives the maximum total reinforcement which means for the same size and loading condition out of all the three codes and span-to-depth ratio, ( $l/D$ ) is an important parameter to decide the amount of reinforcement in the three codes [8].

A computer program-based, analytical, and experimental study was conducted to investigate the effects of loading types and reinforcement ratio on the deflection and crack resistances of the beam, and the results from the three methods were agreed [9]. The experimental study on the effects of shear span-to-depth ratio on shear strength components of RC beams was investigated and the result at small shear span-to-depth ratio ( $a/d$ ),  $V_c$  is much larger than  $V_{cr}$ , while it is the opposite for beams with a large  $a/d$  value [10]. According to the Analysis of Stress and Deflection of rectangular section Cantilever Beam subjected to three different loads point load, UDL load, and UVL independently, and also the

study is validated by ANSYS. The analytical and finite element nodal stress and displacement values were calculated and showed minimum differences between the two methods [11]. In research conducted on mathematical modeling of a beam subjected to different loading conditions, the effects of the moment of inertia ( $I$ ), Young's modulus ( $E$ ), load ( $W$ ), and compressive force ( $P$ ) on deflection variation were formulated [12]. The effect of the shear span-to-depth ( $a/d$ ) ratio on the shear behavior of steel reinforced grout (SRG)-strengthened reinforced concrete (RC) beams is experimentally investigated on Four critical shear spans corresponding to and ratios of 1.60, 2.10, 2.60, and 3.10 on twelve beams cast in four series of three specimens and the result reveals that the efficacy of the SRG significantly increased with an increase in  $a/d$  ratio in deep beams but deteriorated as  $a/d$  ratio increase in slender beams [13].

Reinforced concrete beams, slabs, and stairs are dimensioned to comply with the limits of span-to-depth ratio aimed at satisfying structural, architectural, and economical requirements. Design codes are well-structured documents and standards used as a reference for project work, and academic, and research purposes of a discipline under consideration. Ethiopia as a nation has experienced three national building codes in the last 40 years primarily based on Eurocodes norms with minor and major modifications. Those codes were the Ethiopian Standard Code of Practice, ESCP, 1983-1995, Ethiopian Building Code of Standard, EBCS, 1995-2015, and Ethiopian Standard, ES EN-2015-Onward. Different international building Codal standards recommend different formulas to determine the serviceability and ultimate depth of RC sections.

According to EBCS-2-1995, Section 5.2.2, the minimum effective depth of the beam to control deflection under the satisfaction of serviceability requirements is given as follows [14].

$$d \geq (0.4 + 0.6 \cdot f_{yk} / 400) \cdot l_e / \beta_a \quad (1)$$

Eqn. (1) can be written in the form of span-to-depth ratio as,

$$\frac{l_e}{d} = \frac{400 \beta_a}{160 + 0.6 f_{yk}}$$

Where,

$d$ : minimum depth from serviceability requirement, mm

$f_{yk}$ : characteristics strength of reinforcement, Mpa

$l_e$ : effective length, C/C distance between beam supports

$\beta_a$ : appropriate constant depending on the support condition

**Table 1.** Coefficients  $B_a$ , to take into account support conditions.

| Beam type | Simply supported span | End Span | interior span | Cantilever span |
|-----------|-----------------------|----------|---------------|-----------------|
| $B_a$     | 20                    | 24       | 28            | 10              |

Source: EBCS-2-1995, Table 5.1

According to ES EN 1992-1-1:2015 section 7.4 expression (7.16a), the minimum depth of the beam to control deflection under the satisfaction of serviceability requirements is given as follows [15].

$$l/d = k [11 + 1.5\sqrt{f_{ck}} \cdot \rho_o / \rho + 3.2\sqrt{f_{ck}} \cdot (\rho_o / \rho - 1)^{3/2}], \text{ if } \rho \leq \rho_o \quad (2)$$

Where  $l/d$  is the limit span/depth ratio

$k$  is the factor to take into account the different structural systems;

$\rho_o$  is the reference reinforcement ratio  $= \sqrt{f_{ck}} \cdot 10^{-3}$ ;

$\rho$  is the required tension reinforcement ratio at mid-span to resist moment due to design loads

$f_{ck}$  is cylindrical characteristics compressive strength of the

concrete in MPa units.

For another steel grade, multiply Eqn-(2) by  $\left(\frac{500}{f_{yk} \left(\frac{A_{st,req}}{A_{st,prov}}\right)}\right)$

If the span of the beam is greater than 7m multiply Eqn. (2) by  $7/L_{eff}$

$A_{st, required}$  is assumed to be  $A_{st, provided}$  and  $\rho$  is taken as 0.5% for slightly stressed concrete

**Table 2.** Coefficients  $B_a$ , to take into account Support conditions.

| Beam Type | Simply Supported Span | End Span | Interior Span | Cantilever Span |
|-----------|-----------------------|----------|---------------|-----------------|
| K         | 1.0                   | 1.3      | 1.5           | 0.4             |

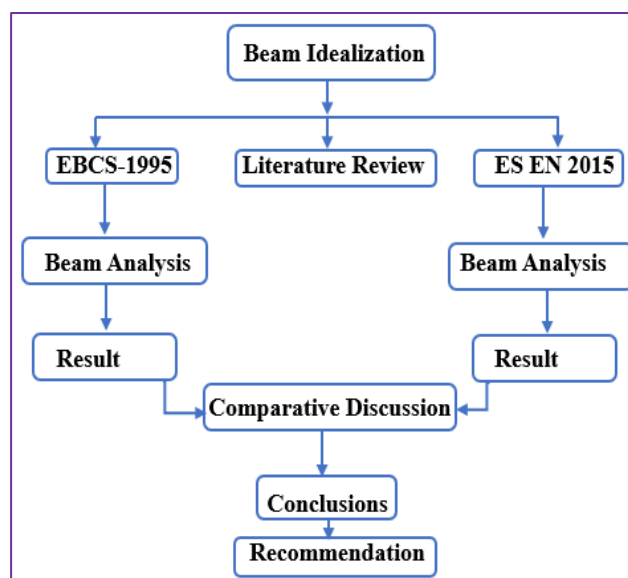
ES EN 1992-1-1:2015, Table 7.4N

EBCS-1995 is the oldest version of Ethiopia's building design standard, which was used for 20 years as a normative design reference for building structures in Ethiopia. However, due to the changes in building design parameters related to material, construction technologies, environmental, complexity of planning, and design requirements EBCS-1995 is no longer used beyond 2015. ES EN 1992-1-1:2015 is currently the adopted building design standard since 2015, which is based on European design norms with minor and major modifications intended to achieve the current and future planning, design, and construction requirements. Some comparative studies among international design codes and among different versions of national building codes have been conducted.

The confusion in not using the new codes effectively and old version codes accordingly causes various planning, designing and cost estimation dilemma and technical errors in current building works. There is wide literature gap that are justifying the gaps of earlier or current design codes and the reasons for design code amendments. The main objective of this comparative analytical study is to show the clear reason for the amendment of the design code considering the most frequent beam element which is interior beam. This codal comparative study will give international research, academic as well as design information importance.

## 2. Methods and Materials

This study is an analytical and comparative study in which the whole process is depicted in Figure 1 below.



**Figure 1.** Study Framework (source: Author 2024).

### 2.1. Model Specification

A slightly reinforced concrete intermediate beam with a C/C effective span of 3m, 3.5m, 4m, 4.5m, 5m, 5.5m, 6m, 6.5m, 7m, 7.5m, and 8m made of steel grade  $f_{yk}$ , 300Mpa, 400Mpa, 500Mpa, 600Mpa, and concrete grade  $f_{cu}$ , 25mpa, longitudinal reinforcement,  $\phi 20$ mm, a shear reinforcement,  $\phi 8$ mm is considered for this study. The beam is supposed to carry LL of 4KN/m<sup>2</sup> from the floor, its self-weight, DL and superimposed dead load of 8KN/m. The beam is analyzed based on linear elastic analysis with 0% moment redistribu-

tion considering the ultimate limit state, ULS and serviceability limit state, and SLS design philosophies. From Codal provision and design experience, the width of the beam is assumed  $D/2$  to  $D/1.5$ , for this study the author assumes  $b =$

$D/2$ , where  $D$  is the total depth and  $B$  is the width of the section. Assuming moderate weather conditions cover for beam 25mm based on EBCS-1995 and 30mm based on ES EN 2015.

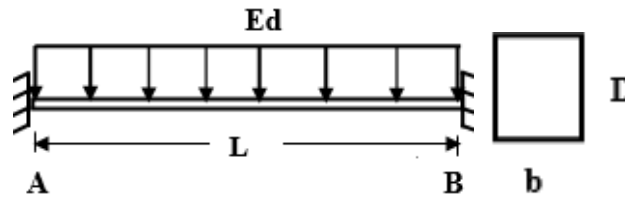


Figure 2. An ideal Model of intermediate beam.

## 2.2. Comparative Parameters

For comparative study of serviceability depth under the two-design code, the following parameters are used.

Table 3. Analytical and Comparative Codal Parameters.

| Comparative Parameters |                | EBCS-1995                            | ES EN-2015   |
|------------------------|----------------|--------------------------------------|--|
| Span-to-depth ratio    | $L/d$          | $400\beta\alpha/(160+0.6f_{yk})$     | $K [11+1.5\sqrt{f_{ck}}*\frac{\rho_0}{\rho} + 3.2\sqrt{f_{ck}}*(\frac{\rho_0}{\rho} - 1)^{3/2}]$ |
| Serviceable depth      | $D$            | $L/(L/d)$                            | $L/(L/d)$  |
| Total depth            | $D$            | $d+CC+\phi_s+\phi_L/2$               | $d+CC+\phi_s+\phi_L/2$   |
| Total width            | $B$            | $D/2$                                | $D/2$  |
| Dead load              | $DL$           | $\gamma_c*D*b$                       | $\gamma_c*D*b$   |
| Live load              | $LL$           | Depends on building's function       | Depends on building's function   |
| Design load            | $W=Ed$         | $1.3DL+1.35SUPDL+1.6LL$              | $1.35DL+1.35SUPDL+1.5LL$   |
| Service load           | $w$            | $DL+LL$                              | $DL+LL$  |
| Moment of inertia      | $I$            | $bD^3/12$                            | $bD^3/12$  |
| Elastic Modulus        | $E_{cm}$       | $9.5(f_{ck}+8)^{1/3}$                | $22((cm/10))^{0.3}$  |
| Calculated Deflection  | $\Delta_{cal}$ | $wl^4/384EI$                         | $wl^4/384EI$   |
| Allowable Deflection   | $\Delta_{all}$ | $L_e/200$                            | $L_e/250$  |
| Maximum Moment         | $Max$          | $Wl^2/12$                            | $Wl^2/12$  |
| Maximum Shear          | $V_{max}$      | $Wl/2$                               | $Wl/2$   |
| Critical design shear  | $V_{cr}$       | $V_{max}(L-2d)/L, d \text{ in m}$    | $V_{max}(L-2d)/L, d \text{ in m}$  |
| Flexural Depth         | $du$           | $\sqrt{M_{max}/0.2952 * b * f_{cd}}$ | $\sqrt{M_{max}/0.2942 * b * f_{cd}}$   |

Source: (EBCS 1995 and ES EN 2015)

## 3. Model Analysis

All essential parameters related to beam depth were analyzed using an excel template under the recommendations of

the two design codes. That parameter includes maximum deflection, allowable deflection, maximum shear, critical design shear, maximum moment, serviceability depth, and ultimate depth.

## 4. Results and Discussions

The numerical values of comparative parameters for a given beam of different span and steel grade are computed

using an Excel sheet with the respective design codes of ES EN-2015 and EBCS-1995. those tabular results are plotted in graphical form for clear comparison.

**Table 4.** Excel results for comparative parameters under EBCS 1995, for  $F_y=300\text{Mpa}$ .

| L(m)                 | 3      | 3.5    | 4      | 4.5    | 5      | 5.5    | 6      | 6.5    | 7      | 7.5    | 8      |
|----------------------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| L/d                  | 33     | 33     | 33     | 33     | 33     | 33     | 33     | 33     | 33     | 33     | 33     |
| d(mm)                | 91.07  | 106.25 | 121.43 | 136.61 | 151.79 | 166.96 | 182.14 | 197.32 | 212.50 | 227.68 | 242.86 |
| D(mm)                | 134.07 | 149.25 | 164.43 | 179.61 | 194.79 | 209.96 | 225.14 | 240.32 | 255.50 | 270.68 | 285.86 |
| b(mm)                | 67.04  | 74.63  | 82.21  | 89.80  | 97.39  | 104.98 | 112.57 | 120.16 | 127.75 | 135.34 | 142.93 |
| DL(KN/m)             | 0.22   | 0.28   | 0.34   | 0.40   | 0.47   | 0.55   | 0.63   | 0.72   | 0.82   | 0.92   | 1.02   |
| LL (KN/m)            | 4      | 4      | 4      | 4      | 4      | 4      | 4      | 4      | 4      | 4      | 4      |
| Ed (KN/m)            | 17.09  | 17.16  | 17.24  | 17.32  | 17.42  | 17.52  | 17.62  | 17.74  | 17.86  | 17.99  | 18.13  |
| w (KN/m)             | 12.22  | 12.28  | 12.34  | 12.40  | 12.47  | 12.55  | 12.63  | 12.72  | 12.82  | 12.92  | 13.02  |
| I (mm <sup>4</sup> ) | 1E+07  | 2E+07  | 3E+07  | 4E+07  | 6E+07  | 8E+07  | 1E+08  | 1E+08  | 2E+08  | 2E+08  | 3E+08  |
| $\Delta_{all}$ (mm)  | 15     | 17.5   | 20     | 22.5   | 25     | 27.5   | 30     | 32.5   | 35     | 37.5   | 40     |
| $\Delta_{cal}$ (mm)  | 6.60   | 8.00   | 9.31   | 10.53  | 11.67  | 12.74  | 13.73  | 14.67  | 15.56  | 16.41  | 17.21  |
| Mmax(KNm)            | 12.82  | 17.52  | 22.99  | 29.23  | 36.28  | 44.16  | 52.87  | 62.45  | 72.93  | 84.33  | 96.68  |
| Vmax(KN)             | 25.64  | 30.03  | 34.48  | 38.98  | 43.54  | 48.17  | 52.87  | 57.65  | 62.51  | 67.46  | 72.51  |
| Vcr(KN)              | 24.08  | 28.21  | 32.39  | 36.61  | 40.90  | 45.25  | 49.66  | 54.15  | 58.72  | 63.37  | 68.11  |
| $\delta_u$ (mm)      | 239.11 | 264.94 | 289.12 | 311.98 | 333.75 | 354.62 | 374.73 | 394.21 | 413.15 | 431.63 | 449.72 |

**Table 5.** Excel result for comparative parameters under ES EN 2015, for  $f_y=300\text{Mpa}$ .

| L(m)                 | 3      | 3.5    | 4      | 4.5    | 5      | 5.5    | 6      | 6.5    | 7      | 7.5    | 8      |
|----------------------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| L/d                  | 44.27  | 44.27  | 44.27  | 44.27  | 44.27  | 44.27  | 44.27  | 44.27  | 44.27  | 41.32  | 38.74  |
| d(mm)                | 67.77  | 79.06  | 90.35  | 101.65 | 112.94 | 124.24 | 135.53 | 146.82 | 158.12 | 181.51 | 206.52 |
| D(mm)                | 115.77 | 127.06 | 138.35 | 149.65 | 160.94 | 172.24 | 183.53 | 194.82 | 206.12 | 229.51 | 254.52 |
| b(mm)                | 57.88  | 63.53  | 69.18  | 74.82  | 80.47  | 86.12  | 91.77  | 97.41  | 103.06 | 114.76 | 127.26 |
| DL(KN/m)             | 0.17   | 0.20   | 0.24   | 0.28   | 0.32   | 0.37   | 0.42   | 0.47   | 0.53   | 0.66   | 0.81   |
| LL (KN/m)            | 4      | 4      | 4      | 4      | 4      | 4      | 4      | 4      | 4      | 4      | 4      |
| Ed (KN/m)            | 17.03  | 17.07  | 17.12  | 17.18  | 17.24  | 17.30  | 17.37  | 17.44  | 17.52  | 17.69  | 17.89  |
| w (KN/m)             | 12.17  | 12.20  | 12.24  | 12.28  | 12.32  | 12.37  | 12.42  | 12.47  | 12.53  | 12.66  | 12.81  |
| I (mm <sup>4</sup> ) | 7.5E+6 | 1.1E+7 | 1.5E+7 | 2.1E+7 | 2.8E+7 | 4E+7   | 4.7E+7 | 6.0E+7 | 7.5E+7 | 1.2E+8 | 1.7E+8 |
| $\Delta_{all}$ (mm)  | 12.00  | 14.00  | 16.00  | 18.00  | 20.00  | 22.00  | 24.00  | 26.00  | 28.00  | 30.00  | 32.00  |
| $\Delta_{cal}$ (mm)  | 11.43  | 14.64  | 17.82  | 20.92  | 23.92  | 26.80  | 29.56  | 32.20  | 34.73  | 30.07  | 26.05  |
| Mmax(KNm)            | 12.77  | 17.43  | 22.83  | 28.99  | 35.91  | 43.61  | 52.11  | 61.41  | 71.53  | 82.92  | 95.43  |
| Vmax(KN)             | 25.54  | 29.88  | 34.25  | 38.65  | 43.09  | 47.58  | 52.11  | 56.68  | 61.31  | 66.33  | 71.57  |
| Vcr(KN)              | 24.39  | 28.53  | 32.70  | 36.90  | 41.15  | 45.43  | 49.75  | 54.12  | 58.54  | 63.12  | 67.88  |

| L(m)   | 3      | 3.5    | 4      | 4.5    | 5      | 5.5    | 6      | 6.5    | 7      | 7.5    | 8      |
|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| du(mm) | 257.26 | 286.88 | 314.66 | 340.92 | 365.89 | 389.78 | 412.73 | 434.87 | 456.31 | 465.58 | 474.31 |

Similarly, for steel grade of 400mpa, 500mpa, and 600mpa all the comparative parameters are analyzed similarly using table 4 and table 5 formats based on the two codes. The results of basic comparative parameters are shown below in tabular and graphical descriptions. The depth from serviceability  $d_o$ , ultimate depth from flexure requirement  $d_{uo}$ , the calculated deflection under service load,  $\Delta_{cal,o}$  and allowable deflection,  $\Delta_{all,o}$ , limiting span to depth ratio,  $l/d_{(o)}$ , the critical design

shear,  $V_{cr,o}$  and maximum design moments,  $M_{max,o}$  based on EBCS 1995 and depth from serviceability  $d_n$ , ultimate depth from flexure requirement  $d_{un}$ , the calculated deflection under service load,  $\Delta_{cal,n}$  and allowable deflection,  $\Delta_{all,n}$ , limiting span to depth ratio,  $l/d_{(n)}$ , the critical design shear,  $V_{cr,n}$  and maximum design moments,  $M_{max,n}$  based on ES EN 2015 are discussed as follow for comparison.

**Table 6.** EBCS 1995 Vs ES EN 2015 Comparative results for different grade of steel.

For steel grade of  $f_yk=300\text{mpa}$

| L(m) | $d_o$  | $d_{uo}$ | $d_n$  | $d_{un}$ | $\Delta_{cal,o}$ | $\Delta_{all,o}$ | $\Delta_{cal,n}$ | $\Delta_{all,n}$ | $V_{cr,o}$ | $V_{cr,n}$ | $M_{max,o}$ | $M_{max,n}$ |
|------|--------|----------|--------|----------|------------------|------------------|------------------|------------------|------------|------------|-------------|-------------|
| 3    | 91.07  | 239.11   | 67.77  | 257.26   | 6.605            | 15               | 11.43            | 12               | 24.08      | 24.39      | 12.82       | 12.77       |
| 3.5  | 106.25 | 264.94   | 79.06  | 286.88   | 8.003            | 17.5             | 14.64            | 14               | 28.21      | 28.53      | 17.52       | 17.43       |
| 4    | 121.43 | 289.12   | 90.35  | 314.66   | 9.312            | 20               | 17.82            | 16               | 32.39      | 32.70      | 22.99       | 22.83       |
| 4.5  | 136.61 | 311.98   | 101.65 | 340.92   | 10.533           | 22.5             | 20.92            | 18               | 36.61      | 36.90      | 29.77       | 28.99       |
| 5    | 151.79 | 333.75   | 112.94 | 365.89   | 11.672           | 25               | 23.92            | 20               | 40.90      | 41.15      | 36.28       | 35.91       |
| 5.5  | 166.96 | 354.62   | 124.24 | 389.78   | 12.736           | 27.5             | 26.80            | 22               | 45.25      | 45.43      | 44.16       | 43.61       |
| 6    | 182.14 | 374.73   | 135.53 | 412.73   | 13.734           | 30               | 29.56            | 24               | 49.66      | 49.75      | 52.87       | 52.11       |
| 6.5  | 197.32 | 394.21   | 146.82 | 434.87   | 14.673           | 32.5             | 32.20            | 26               | 54.15      | 54.12      | 62.45       | 61.41       |
| 7    | 212.50 | 413.15   | 158.12 | 456.31   | 15.562           | 35               | 34.73            | 28               | 58.72      | 58.54      | 72.93       | 71.53       |
| 7.5  | 227.68 | 431.63   | 181.51 | 465.58   | 16.407           | 37.5             | 30.07            | 30               | 63.37      | 63.12      | 84.33       | 82.92       |
| 8    | 242.86 | 449.72   | 206.52 | 474.31   | 17.215           | 40               | 26.05            | 32               | 68.11      | 67.88      | 96.68       | 95.43       |

For steel grade of  $f_yk=400\text{mpa}$

| L(m) | $d_o$  | $d_{uo}$ | $d_n$  | $d_{un}$ | $\Delta_{cal,o}$ | $\Delta_{all,o}$ | $\Delta_{cal,n}$ | $\Delta_{all,n}$ | $V_{cr,o}$ | $V_{cr,n}$ | $M_{max,o}$ | $M_{max,n}$ |
|------|--------|----------|--------|----------|------------------|------------------|------------------|------------------|------------|------------|-------------|-------------|
| 3    | 107.14 | 226.44   | 90.35  | 236.00   | 4.219            | 15               | 5.64             | 12               | 23.91      | 24.14      | 12.87       | 12.84       |
| 3.5  | 125.00 | 250.42   | 105.41 | 262.03   | 5.015            | 17.5             | 6.94             | 14               | 28.05      | 28.28      | 17.62       | 17.56       |
| 4    | 142.86 | 272.91   | 120.47 | 286.45   | 5.748            | 20               | 8.18             | 16               | 32.24      | 32.48      | 23.15       | 23.04       |
| 4.5  | 160.71 | 294.21   | 135.53 | 309.55   | 6.424            | 22.5             | 9.35             | 18               | 36.51      | 36.72      | 29.49       | 29.31       |
| 5    | 178.57 | 314.55   | 150.59 | 331.57   | 7.049            | 25               | 10.46            | 20               | 40.85      | 41.03      | 36.66       | 36.39       |
| 5.5  | 196.43 | 334.12   | 165.65 | 352.69   | 7.631            | 27.5             | 11.50            | 22               | 45.28      | 45.41      | 44.70       | 44.29       |
| 6    | 214.29 | 353.04   | 180.71 | 373.06   | 8.176            | 30               | 12.49            | 24               | 49.80      | 49.85      | 53.63       | 53.05       |
| 6.5  | 232.14 | 371.44   | 195.77 | 392.79   | 8.691            | 32.5             | 13.42            | 26               | 54.41      | 54.37      | 63.48       | 62.68       |
| 7    | 250.00 | 389.40   | 210.83 | 411.98   | 9.179            | 35               | 14.31            | 28               | 59.13      | 58.98      | 74.30       | 73.22       |

| L(m) | do     | duo    | dn     | dun    | $\Delta_{cal,o}$ | $\Delta_{all,o}$ | $\Delta_{cal,n}$ | $\Delta_{all,n}$ | Vcr,o | Vcr,n | Mmax,o | Mmax,n |
|------|--------|--------|--------|--------|------------------|------------------|------------------|------------------|-------|-------|--------|--------|
| 7.5  | 267.86 | 407.00 | 242.02 | 420.34 | 9.645            | 37.5             | 12.16            | 30               | 63.97 | 63.91 | 86.11  | 85.40  |
| 8    | 285.71 | 424.30 | 275.36 | 428.62 | 10.094           | 40               | 10.39            | 32               | 68.92 | 69.15 | 98.96  | 99.01  |

For steel grade of  $f_y k = 500 \text{ mpa}$

| L(m) | do     | duo    | dn     | dun    | $\Delta_{cal,o}$ | $\Delta_{all,o}$ | $\Delta_{cal,n}$ | $\Delta_{all,n}$ | Vcr,o | Vcr,n | Mmax,o | Mmax,n |
|------|--------|--------|--------|--------|------------------|------------------|------------------|------------------|-------|-------|--------|--------|
| 3    | 123.21 | 215.73 | 112.94 | 219.54 | 2.82             | 15.00            | 3.10             | 12.00            | 23.75 | 23.91 | 12.94  | 12.93  |
| 3.5  | 143.75 | 238.26 | 131.77 | 262.03 | 3.31             | 17.50            | 3.71             | 14.00            | 27.90 | 27.88 | 17.73  | 17.71  |
| 4    | 164.29 | 259.43 | 150.59 | 265.25 | 3.75             | 20.00            | 4.28             | 16.00            | 32.12 | 32.30 | 23.33  | 23.29  |
| 4.5  | 184.82 | 279.55 | 169.41 | 286.28 | 4.15             | 22.50            | 4.81             | 18.00            | 36.44 | 36.61 | 29.77  | 29.70  |
| 5    | 205.36 | 298.83 | 188.24 | 306.40 | 4.52             | 25.00            | 5.31             | 20.00            | 40.85 | 41.01 | 37.09  | 36.96  |
| 5.5  | 225.89 | 317.44 | 207.06 | 325.78 | 4.87             | 27.50            | 5.77             | 22.00            | 45.37 | 45.51 | 45.31  | 45.12  |
| 6    | 246.43 | 335.51 | 225.88 | 344.58 | 5.19             | 30.00            | 6.21             | 24.00            | 50.01 | 50.12 | 54.48  | 54.20  |
| 6.5  | 266.96 | 353.15 | 244.71 | 362.88 | 5.50             | 32.50            | 6.62             | 26.00            | 54.77 | 54.83 | 64.65  | 64.24  |
| 7    | 287.50 | 370.45 | 263.53 | 380.79 | 5.80             | 35.00            | 7.02             | 28.00            | 59.67 | 59.67 | 75.85  | 75.29  |
| 7.5  | 308.04 | 387.48 | 302.52 | 389.15 | 6.08             | 37.50            | 5.91             | 30.00            | 64.72 | 65.07 | 88.14  | 88.47  |
| 8    | 328.57 | 404.29 | 344.20 | 397.81 | 6.36             | 40.00            | 5.02             | 32.00            | 69.92 | 70.91 | 101.57 | 103.44 |

For steel grade of  $f_y k = 600 \text{ mpa}$

| L(m) | do     | duo    | dn     | dun    | $\Delta_{cal,o}$ | $\Delta_{all,o}$ | $\Delta_{cal,n}$ | $\Delta_{all,n}$ | Vcr,o | Vcr,n | Mmax,o | Mmax,n |
|------|--------|--------|--------|--------|------------------|------------------|------------------|------------------|-------|-------|--------|--------|
| 3    | 139.29 | 206.55 | 135.53 | 206.36 | 1.96             | 15.00            | 1.85             | 12.00            | 23.59 | 23.70 | 13.00  | 13.03  |
| 3.5  | 162.50 | 227.91 | 158.12 | 228.15 | 2.27             | 17.50            | 2.17             | 14.00            | 27.76 | 27.88 | 17.85  | 17.88  |
| 4    | 185.71 | 248.05 | 180.71 | 248.70 | 2.55             | 20.00            | 2.47             | 16.00            | 32.02 | 32.17 | 23.53  | 23.58  |
| 4.5  | 208.93 | 267.25 | 203.30 | 268.30 | 2.81             | 22.50            | 2.74             | 18.00            | 36.40 | 36.57 | 30.09  | 30.15  |
| 5    | 232.14 | 285.72 | 225.88 | 287.15 | 3.04             | 25.00            | 2.99             | 20.00            | 40.89 | 41.08 | 37.56  | 37.64  |
| 5.5  | 255.36 | 303.62 | 248.47 | 305.41 | 3.26             | 27.50            | 3.23             | 22.00            | 45.52 | 45.74 | 46.00  | 46.09  |
| 6    | 278.57 | 321.08 | 271.06 | 323.22 | 3.47             | 30.00            | 3.46             | 24.00            | 50.29 | 50.53 | 55.44  | 55.55  |
| 6.5  | 301.79 | 338.20 | 293.65 | 340.67 | 3.67             | 32.50            | 3.67             | 26.00            | 55.23 | 55.49 | 65.95  | 66.09  |
| 7    | 325.00 | 355.07 | 316.24 | 357.86 | 3.86             | 35.00            | 3.88             | 28.00            | 60.33 | 60.61 | 77.59  | 77.74  |
| 7.5  | 348.21 | 371.74 | 363.03 | 366.70 | 4.05             | 37.50            | 3.26             | 30.00            | 65.61 | 66.56 | 90.41  | 92.11  |
| 8    | 371.43 | 388.28 | 413.05 | 376.17 | 4.23             | 40.00            | 2.77             | 32.00            | 71.09 | 73.13 | 104.49 | 108.73 |

The deflection and depth of a beam are represented on the y-axis in mm while the span of a beam is represented on the x-axis in m. The variation of depth and deflection under different steel grades is presented below.



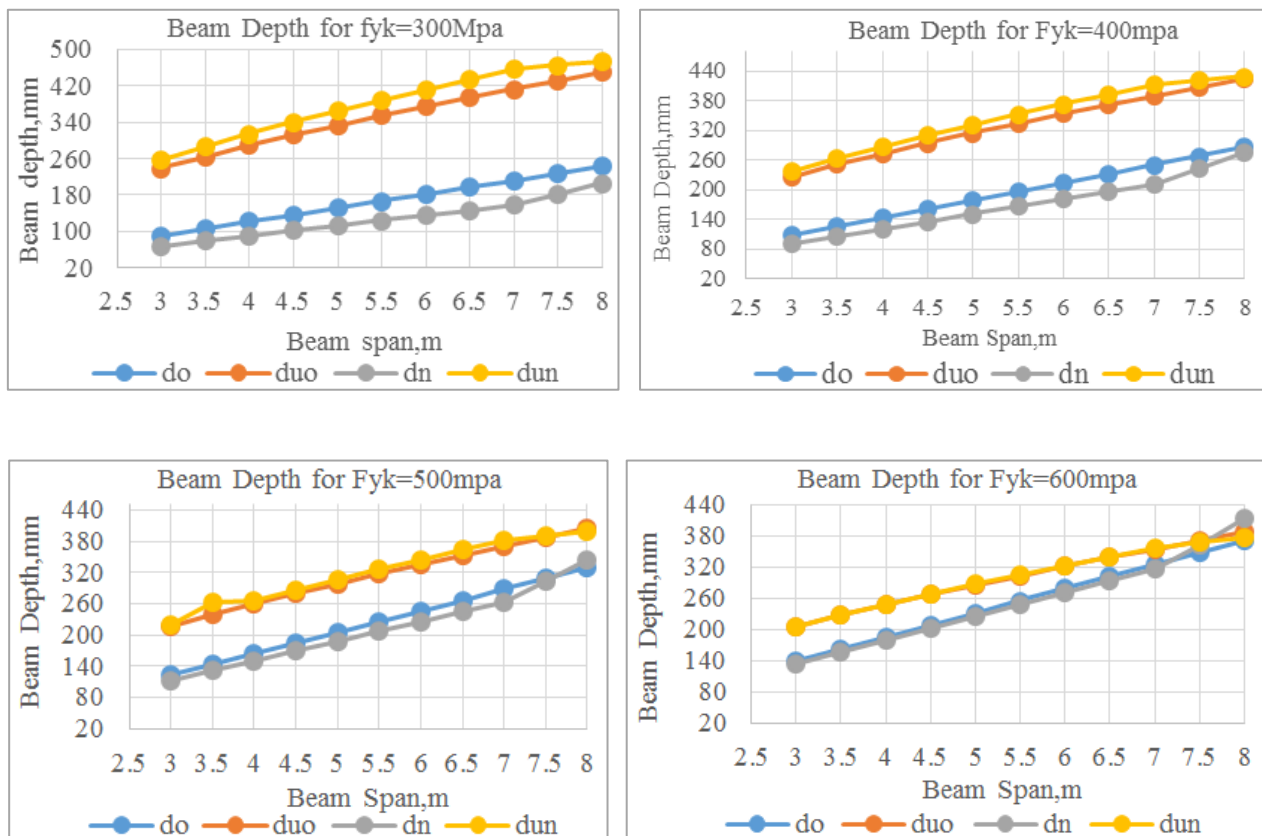


Figure 3. Variation of serviceability and ultimate beam depth.

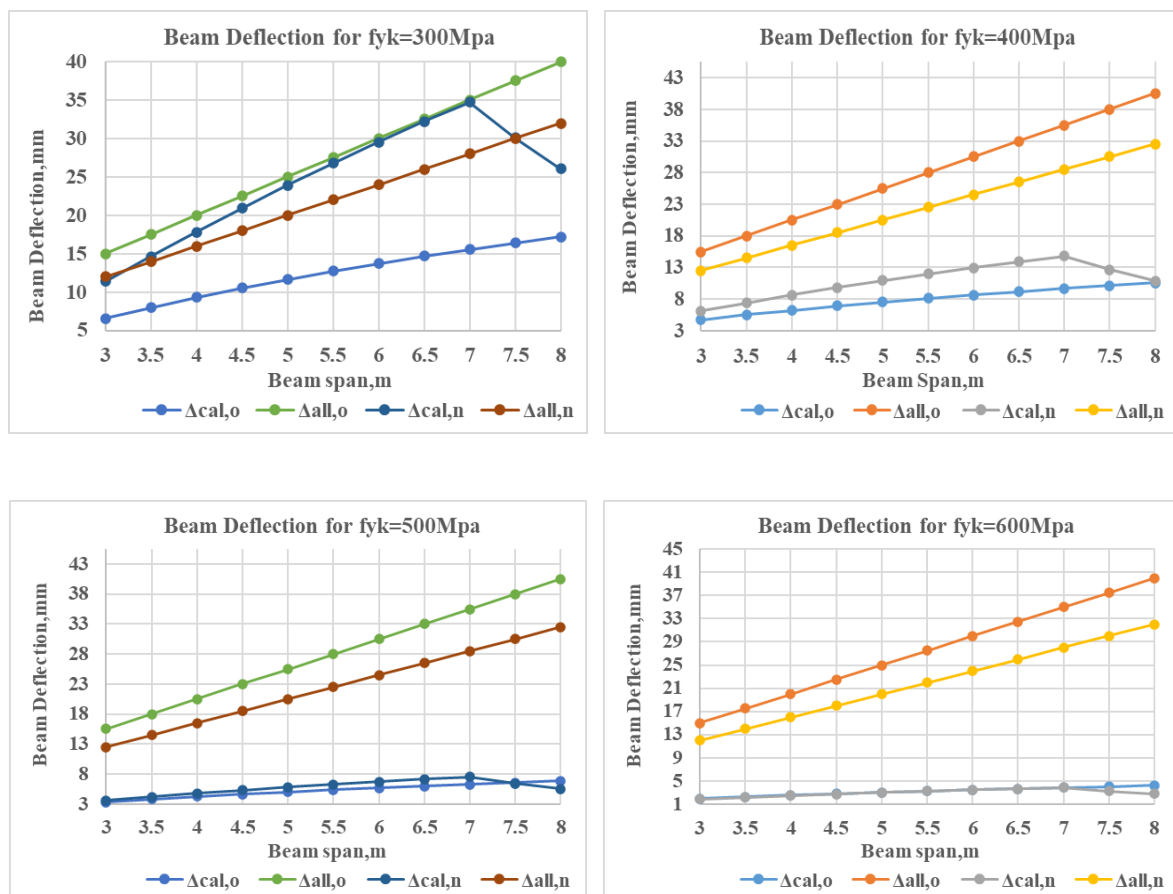


Figure 4. Variation of maximum and allowable beam deflection.



The effective depth to span ratio at different steel grades is calculated. The result shows that the depth calculated from EBCS 1995 is independent of steel grade while the depth calculated from ES EN 2015 depends on the grade of steel.

**Table 7.** Span-to-depth Ratio for EBCS 1995,  $l/d(o)$  and ES EN 2015,  $l/d(n)$ .

| L(m) | fyk=300mpa |          | fyk=400mpa |          | fyk=500mpa |          | fyk=600mpa |          |
|------|------------|----------|------------|----------|------------|----------|------------|----------|
|      | $l/d(o)$   | $l/d(n)$ | $l/d(o)$   | $l/d(n)$ | $l/d(o)$   | $l/d(n)$ | $l/d(o)$   | $l/d(n)$ |
| 3    | 32.94      | 44.27    | 28.00      | 33.20    | 24.35      | 26.56    | 21.54      | 22.14    |
| 3.5  | 32.94      | 44.27    | 28.00      | 33.20    | 24.35      | 26.56    | 21.54      | 22.14    |
| 4    | 32.94      | 44.27    | 28.00      | 33.20    | 24.35      | 26.56    | 21.54      | 22.14    |
| 4.5  | 32.94      | 44.27    | 28.00      | 33.20    | 24.35      | 26.56    | 21.54      | 22.14    |
| 5    | 32.94      | 44.27    | 28.00      | 33.20    | 24.35      | 26.56    | 21.54      | 22.14    |
| 5.5  | 32.94      | 44.27    | 28.00      | 33.20    | 24.35      | 26.56    | 21.54      | 22.14    |
| 6    | 32.94      | 44.27    | 28.00      | 33.20    | 24.35      | 26.56    | 21.54      | 22.14    |
| 6.5  | 32.94      | 44.27    | 28.00      | 33.20    | 24.35      | 26.56    | 21.54      | 22.14    |
| 7    | 32.94      | 44.27    | 28.00      | 33.20    | 24.35      | 26.56    | 21.54      | 22.14    |
| 7.5  | 32.94      | 41.32    | 28.00      | 30.99    | 24.35      | 24.79    | 21.54      | 20.66    |
| 8    | 32.94      | 38.74    | 28.00      | 29.05    | 24.35      | 23.24    | 21.54      | 19.37    |

## 5. Conclusions

- 1) EBCS 1995 is independent of concrete grade in beam depth determination while ES EN 2015 is highly dependent on the grade of concrete and level of stressing the concrete for use.
- 2) At a higher grade of steel EBCS 1995 gives a little higher serviceable depth for lower spans than ES EN 2015 which makes uneconomical design in steel and concrete proportioning.
- 3) Under a given concrete grade and variable steel grade EBCS-1995 quickly satisfies both serviceability and flexural requirements than ES EN 2015.
- 4) Under a given service load EBCS 1995 gives relatively lesser deflection than ES EN 2015.
- 5) Allowable deflection as per ES EN 2015 is restricted to less than 20% allowed as per EBCS 1995 to higher spans.
- 6) EBCS 1995 gives higher section depth, for lesser critical design shear, and lesser ultimate moment than ES EN 2015 for different steel and concrete grades which results in uneconomical design.
- 7) EBCS 1995 better satisfies serviceability depth for a given span and concrete grade than ES EN 2015, while ES EN 2015 better satisfies ultimate depth requirement than EBCS 1995.
- 8) Under a given span up to 7m, shows the smaller value of under  $l/d$  EBCS-1995 than ES EN 2015 and for a

beam span greater than 7m,  $l/d$  ratios are reduced from ES EN-2015 consideration.

- 9) ES EN-2015 gives an economical and effective beam width under a given  $l/D$  ratio than EBCS 1995.
- 10) When the grade of steel increase  $l/d$  ratio in both codes decreases while for ES EN 2015  $l/d$  ratio decreases for a beam span greater than 7m.
- 11) Both design codes have no mechanism for the calculation to reduce the cross-section of the beam in the subsequent uppermost story to minimize cost and self-weight effects.
- 12) Generally, EBCS 1995 is uneconomical for shear and moment design which needs more section depth, especially for longer spans, and also the code is independent of concrete grade to determine the depth of the section while ES EN 2015 provides smaller but effective serviceable depth by limiting smaller deflection values.

## 6. Recommendations

- 1) Due to self-weight and the live load reduction in the subsequent top stories, the depth of the beam should be decreased as compared to lower story beam depths, but most code formulas don't consider the effect of story in-depth determination. This should be studied.
- 2) A study should be done on how to select the grade of steel and the grade of concrete to have a better combination of steel-concrete grades to achieve a strong and

economical RC structure.

## Highlights of the Research

- 1) Design codes and standards
- 2) Interior beam
- 3) Ultimate depth
- 4) Serviceability depth

## Abbreviations

EBCS: Ethiopian Building Code of Standard  
 ESCP: Ethiopian Standard Code of Practice  
 ES EN: Ethiopian Standard Euro Norm  
 DL: Ddead Load  
 KN: Kilo Newton  
 LL: Live Load  
 MPa: Mega Pascal  
 RC: Reinforced Concrete  
 UDL: Uniformly Distributed Load  
 UVL: uniformly Varying Load

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## Data Availability Statement

The data will be made available upon the request

## Conflicts of Interest

The author declares no conflicts of interest.

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